

# Phreatic Surface Estimation In MSE Wall With Geocomposite Back Drainage

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## Research Article

**Keywords:** MSE wall, protected area, maximum water level, geonet transmissivity, linear association

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1                   **PHREATIC SURFACE ESTIMATION IN MSE WALL WITH GEOCOMPOSITE**

2   **BACK DRAINAGE**

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35 **ABSTRACT**

36 This study proposes a simple mathematic model for approximating the level of phreatic surface  
37 inside the protected zone in mechanical stabilized earth wall with back drain installation though  
38 the position of phreatic surface at the drainage interface ( $h_o$ ) which reflects the maximum level  
39 of phreatic surface in the protected zone. The proposed model was established based on dataset  
40 taken from 180 simulation cases caried out in Plaxis environment. Regression results present a  
41 combination of significant effects and major role to maximum water level in the protected zone  
42 ( $h_o$ ) of a ratio of length from upstream water to the drainage face to the wall height ( $L/H$ ), a  
43 soil permeabilities coefficient ( $k$ ) and a transmissivity of the drainage material ( $T_{net}$ ). The  
44 proposed model can facilitate design of drainage material to achieve desired level of phreatic  
45 surface in the protected zone.

46 **Keywords:** MSE wall, protected area, maximum water level, geonet transmissivity, linear  
47 association

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## 60 INTRODUCTION

61 Although drainage system was properly installed behind mechanical stabilized earth (MSE)  
62 wall, failures happened during long term rainfall have been mentioned in many reports (Yoo  
63 and Jung, 2006; Koerner and Koerner, 2018; Zhang et al., 2015; Koerner and Koerner, 2015;  
64 Vahedifard et al., 2017). The wide distribution of high water content in the protected zone was  
65 a major source for many types of failure (Zhang et al., 2015; Chinkulkijniwat et al., 2016). To  
66 narrow the high water content zone, the backfill soil must consist of least fine particle and the  
67 level of phreatic surface inside the protected zone must be minimized. Good estimation of  
68 phreatic level inside the protected zone is, therefore, vital for design of MSE wall. This study  
69 focuses accurate estimation of phreatic level inside the protected zone though the high of  
70 phreatic surface at the drainage interface in the protected zone ( $h_o$ ). The  $h_o$  is considered as the  
71 maximum level of phreatic surface in the protected zone and reflects the effectiveness of the  
72 drainage system.

73 Previous reports, i.e. Koerner and Koerner (2018), Koerner and Koerner (2015). Vahedifard et  
74 al. (2017), indicated that there were many factors influencing the  $h_o$  variation such as soil  
75 hydrological properties, properties of drainage material, and the wall dimensions. However,  
76 none of the previous attempts had been devoted to estimate the magnitude of  $h_o$   
77 comprehensively. To date, engineers design the required transmissivity of drainage layer using  
78 a classical Dupuit's formular with an assumption that the phreatic level inside the protected  
79 zone is zero. Previous study from the authors (Chinkulkijniwat et al., 2016, Bui Van et al.,  
80 2017, La Duong et al., 2021) reports none zero phreatic level inside the protected zone even  
81 after assigning transmissivity of drainage layer greater than that provided by Dupuit's equation.  
82 For a given wall geometry of homogeneous soil, La Duong et al. (2021) reported linear  
83 relationship between  $h_o$  and logarithm of geonet transmissivity ( $T_{net}$ ). Furthermore, the gradient  
84 of the  $h_o$ - $\log(T_{net})$  relationship was found governed by the permeability coefficient of the

85 upstream soil. This paper extends this important finding to propose a closed form equation for  
 86  $h_o$  estimation. Data used in this study were gathered from 180 sets of numerical calculation  
 87 extracted from well calibrated Plaxis-2D model (Chinkulkijniwat et al., 2016). Steady-state  
 88 flow conditions were focused in this study to quantify the final state of ground water flow in  
 89 MSE wall .The proposed equation will assist drainage design in MSE wall with back drain  
 90 installation.

## 91 **METHODOLOGY**

### 92 **Research background**

93 Soil-water model is based on van Genuchten model (Eq .1a) (van Genuchten, 1981) and van  
 94 Genuchten -Mualem model (Eq .1b), which is an integration of the van Genuchten model with  
 95 the Mualem hypothesis (Mualem, 1976), were employed to approximate the water retention  
 96 curve and permeability functions for every porous media in the MSE wall problem .The models  
 97 gave the following equations :

$$98 \quad S_e = \frac{S - S_{res}}{S_{sat} - S_{res}} = [1 + (\alpha |h_p|)^n]^{-m} \quad (1a)$$

$$99 \quad k_r(S_e) = S_e^{0.5} [1 - (1 - S_e^{1/m})^m]^2 \quad (1b)$$

100 In the above equations,  $S_e$  is effective degree of saturation [-],  $S$  is degree of saturation [-],  $S_{res}$   
 101 is residual saturation at very high values of suction [-],  $S_{sat}$  is the degree of saturation at  
 102 saturated state [-],  $h_p$  is matric suction head [m], and  $k_r$  is the relative permeability coefficient  
 103 [m/sec],  $\alpha$  [ $m^{-1}$ ] and  $n$  [-] are fitting parameters which represent respectively the air-entry head  
 104 of the soil and the rate of water extraction from the soil once the air entry head has been  
 105 exceeded, while  $m$  [-] is assigned the value  $1 - 1/n$  [7].

### 106 **Simulation scenarios for linear association analysis**

107 Well calibrated MSE wall with back drain installation model in Plaxis environment (Figure 1)  
 108 reported by Chinkulkijniwat et al. (2016) was employed to approximate the maximum phreatic

109 level in the protected zone of MSE wall ( $h_o$ ). The upstream water level in all calculations was  
 110 set equal to the wall height to imitate vital scenario of the MSE wall in mountainous terrain,  
 111 where heavy rainfall could raise the upstream water level to equal height of the wall. In this  
 112 study, the upstream-, foundation-, and backfill-soils were assigned identically. Six soil types;  
 113 including coarse sand (Konukcu et al., 2004), sandy soil (Chinkulkijniwat et al., 2016), clayey  
 114 soil (Szymkiewicz et al., 2015), lateritic soil (Bui Van et al., 2017) and clay (Koerner and  
 115 Koerner, 2015), were assigned to perform the calculation. Saturated permeability coefficient  
 116 and van Genuchten parameters these soils are given in Table 1. As for the wall dimensions  
 117 ratio; including the distance from the wall base to the impervious boundary to the wall height  
 118 ( $D/H$ ), the protected zone width to the wall height ( $W/H$ ), and the distance from the upstream  
 119 water source to the drainage face to the wall height ( $L/H$ ), La Duong et al. (2021) reports that  
 120 except the dimension ratio  $L/H$ , other wall dimension ratios play small to negligible role to the  
 121 magnitude of  $h_o/H$ . Accordingly, for wall dimension set up in this study, the wall height ( $H$ ),  
 122 distance from the wall base to the impervious boundary ( $D$ ), and the protected zone width ( $W$ )  
 123 were fixed at 2.0 m, 0.8 m, and 2.0 m, respectively. The shape parameter  $L$  was varied in range  
 124 from  $L/H$  of 1.0 to  $L/H$  of 2.5 as stated in Table 2. Geonet transmissivity was controlled by  
 125 geonet thickness ( $t_{net}$ ) and geonet permeability ( $k_{net}$ ) through the relationship written in Eq. 2,

$$126 \quad T_{net} = k_{net} \times t_{net} \quad (2),$$

127 where  $T_{net}$  is geonet transmissivity ( $m^2/sec$ ),  $t_{net}$  is geonet thickness (m) and  $k_{net}$  is geonet  
 128 permeability (m/sec). The assigned hydrological properties of geonet as thickness ( $t_{net}$ ),  
 129 permeability ( $k_{net}$ ) are also given in **Table 2**. Totally, 180 calculation cases were conducted in  
 130 this study. Within this dataset, 18 calculation results yielding  $h_o$  value of 0.001 m were  
 131 eliminated from the analysis. Since the smallest  $h_o$  readable from the calculations was 0.001  
 132 m, including this dataset might deviate the analyzed result.

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## 134 RESULTS AND DISCUSSION

135 The relationships between  $h_o$  and  $\log(T_{net})$  for coarse sand, sandy soil, clayey sand, lateritic  
136 soil, and clay extracted from Plaxis calculation are respectively shown in **Fig. 2a, 2b, 2c, 2d,**  
137 **and 2e.** The drop of  $h_o$  with the increase of  $\log(T_{net})$  reflects the greater amount of water allow  
138 to flow along the drainage channel. Linear regression was employed to fit the  $h_o - \log(T_{net})$   
139 relationship. All plots reflect themselves best fit with linear association via the coefficient of  
140 determination  $r^2$  greater than 0.96. Although the variation of  $h_o$  with  $\log(T_{net})$  was well fitted  
141 through linear regression, no further correlation was found along these plots. Since the  
142 permeability coefficient of the upstream soil ( $k$ ) plays important role to the drop of  $h_o$  with  
143 increasing  $T_{net}$  (La Duong et al, 2021), the permeability coefficient ( $k$ ) was included in the  $T_{net}$   
144 term as  $\log(T_{net}/k)$  and plotted with  $\log(h_o)$  as shown in **Figure 3.** The plots exhibit similar  
145 pattern for all values of shape parameter  $L$ , hence the shape parameter  $L$  must be included to  
146 normalize the data. After trial and error, the term  $\log(T_{net}/k)$  was transformed to  
147  $\log(T_{net}/k^{(10+L/H)/10})$  and the variation of  $\log(h_o)$  with  $\log(T_{net}/k^{(10+L/H)/10})$  exhibit unique  
148 relationship with the coefficient of determination  $r^2$  of 0.93 as shown in **Figure 4.** The equation  
149 for  $h_o$  estimation in MSE wall with geocomposite back drainage is, hence, delivered as:

$$150 \text{Log}(h_o) = -0.16 - 0.56 \log(T_{net}/k^{(10+L/H)/10}) \quad (3)$$

151 To verify the above equation, 12 extra Plaxis calculations having the influence variables were  
152 randomly assigned to the model. **Table 3** presents variation of influence variables and the  
153 corresponding  $h_o$  values extracted from these extra calculations. The  $h_o$  values yield from Eq.  
154 3 are also presented in this table. Comparison between  $h_o$  values calculated from Plaxis and  
155 that from Eq. 3 is shown in **Figure 5.** The coefficient of determination  $r^2$  along 1:1 line is 0.96  
156 indicating level of accuracy of the  $h_o$  prediction using Eq. 3.

## 157 CONCLUSION

158 Following points are drawn from this study:

- 159 • Simple mathematic model for approximating the maximum water level in the protected  
160 zone ( $h_o$ ) for mechanical stabilized earth wall with back drain installation was  
161 established through dataset calculated from a well calibrated model in Plaxis  
162 environment.
- 163 • Based on previous report (La Duong et al., 2021), important parameters playing role to  
164 the change of  $h_o$  are 1) permeability coefficient of upstream soil ( $k$ ), 2) transmissivity  
165 of the back drain ( $T_{net}$ ), and 3) a ratio of the distance from the upstream water source to  
166 the drainage face to the wall height ( $L/H$ ). Hence, the model was established based on  
167 variation of these 3 parameters.
- 168 • The proposed equation was established based on identical soil at the upstream- and  
169 protection-zones. In practical situation, the soil located in protected zone always  
170 possesses its permeability coefficient no less than that of the upstream soil. According  
171 to Bui Van et al. (2017) and La Duong et al. (2021), if the soil in the protected zone  
172 possesses more permeable than the soil in the upstream side does, the flow path  
173 reflection results in the lower phreatic surface in the protected for the more permeable  
174 soil in the protected zone than that for the less permeable soil in the protected zone. As  
175 such, magnitude of  $h_o$  approximated from the proposed equation is conceptually no  
176 lower than that take place in MSE wall having higher soil permeability in the protected  
177 zone than that in the upstream side, i.e. the propose equation yields conservative results.

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## 181 **STATEMENT FOR CONFLICT OF INTEREST**

182 On behalf of all authors, the corresponding author states that there is no conflict of interest



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**Table 1.** Permeability coefficient and van Genuchten parameters of the studied materials.

Material	Permeability (m/sec)	$\alpha$ ( $m^{-1}$ )	n (-)	$S_{sat}$ (-)	$S_{res}$ (-)
Coarse sand	$1.3 \times 10^{-3}$	49.36	1.53	1.0	0.002
Sandy soil	$1.97 \times 10^{-4}$	20	1.5	1.0	0.03
Clayey sand	$4.1 \times 10^{-5}$	12.4	2.28	1.0	0.14
Lateritic soil	$4.0 \times 10^{-6}$	0.8	1.4	1.0	0.03
Clay	$5.56 \times 10^{-7}$	0.08	$8.0 \times 10^{-5}$	0.74	0.12
Geotextile	0.023 (0.0037) <sup>a</sup>	20	2.5	0.8	0.03
Geonet	0.8	600	40	1.0	0.0

<sup>a</sup> Permeability of geotextile in lateral direction.

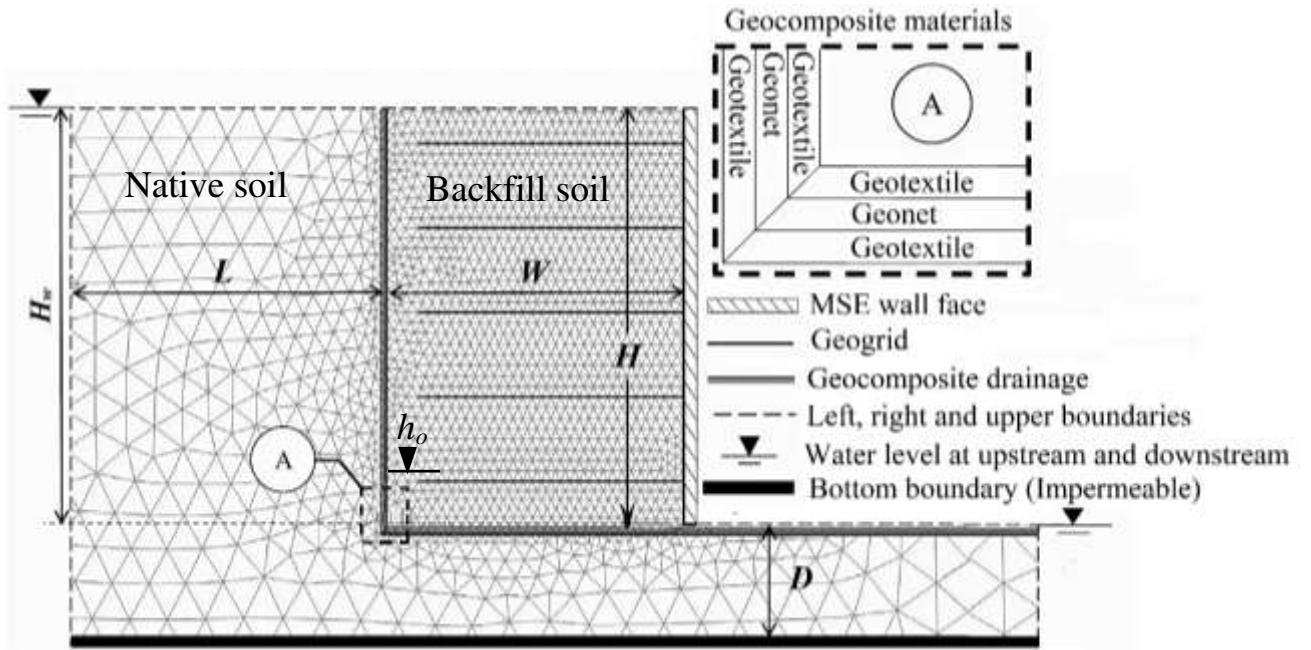
**Table 2.** Variable setup of 180 simulations in Plaxis environment

Scenario	Prescribed soil	Reference
<i>A</i>	Coarse sand	Konukcu et al. (2004)
<i>B</i>	Sandy soil	Chinkulkijniwat et al. (2016)
<i>C</i>	Clayey sand	Szymkiewicz et al. (2015)
<i>D</i>	Lateritic soil	Bui Van et al. (2017)
<i>E</i>	Clay	Koerner and Koerner (2015)
Fixed parameter		
<i>W</i> (m)	Protected zone width	1.6
<i>H</i> (m)	MSE wall height	2.0
<i>D</i> (m)	Distance from the wall base to the impervious boundary	0.8
Varied parameter Definition		Varied value
<i>L</i> (m)	Length from upstream water to the drainage face	2.0, 3.0, 4.0, 5.0
<i>t<sub>net</sub></i> (mm)	Geonet thickness	10, 15, 20
<i>k<sub>net</sub></i> (m/sec)	Geonet permeability	0.8, 0.08, 0.008

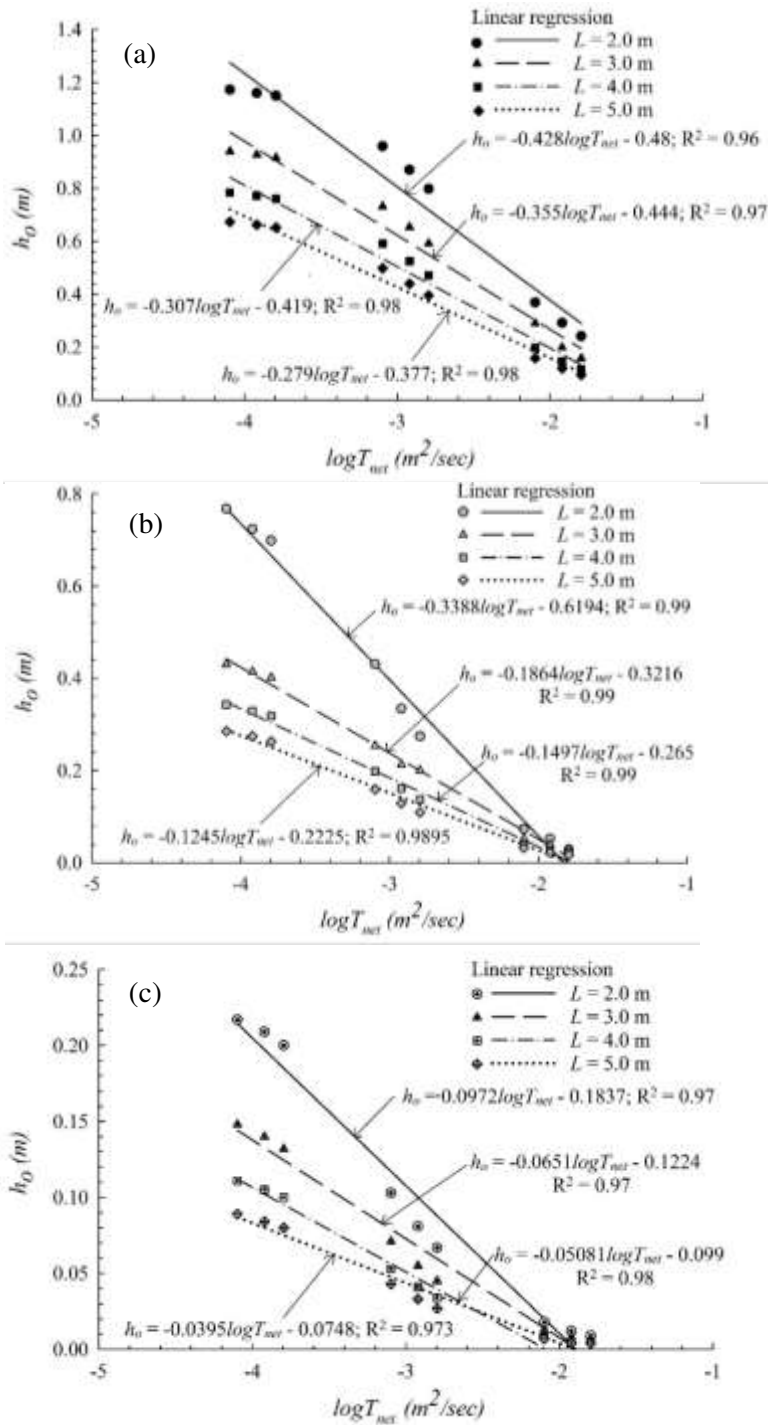
Upstream water level ( $H_w$ ) is kept as constant 2.0 for all simulation cases

**Table 3.** Assigned variables in 12 verified cases and the corresponding  $h_o$  values from Plaxis calculation and that from the proposed equation.

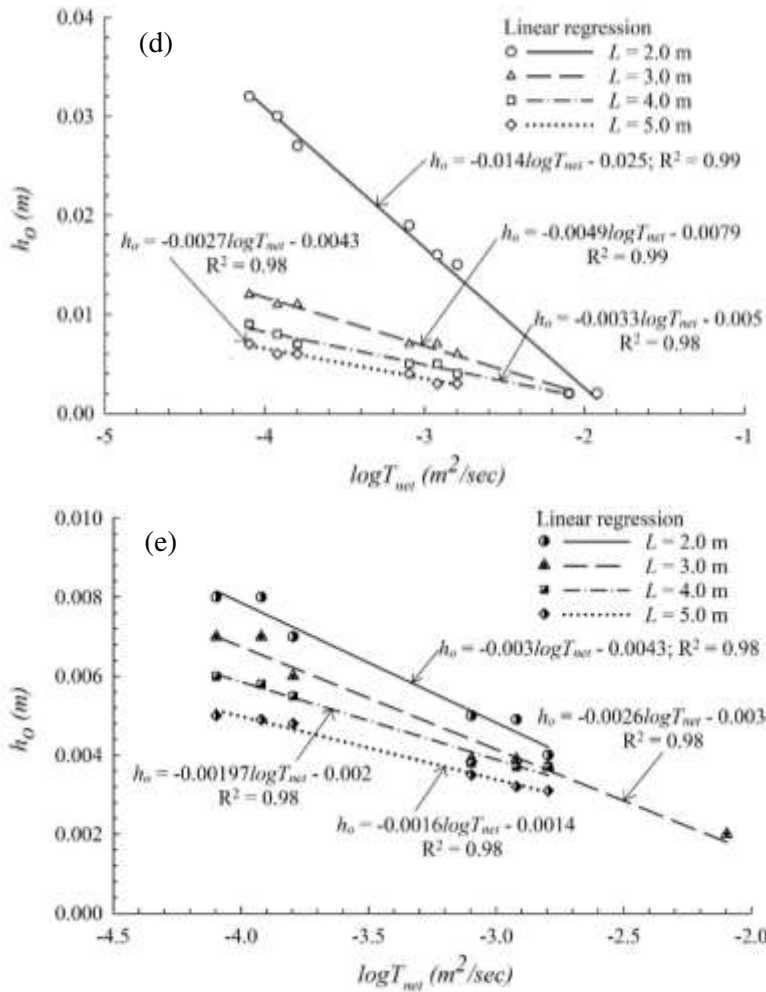
Soil type and its permeability	Case no.	$H$ (m)	$L$ (m)	$T_{net}$ (m <sup>2</sup> /sec)	$h_o$ (m) (Plaxis)	$h_o$ (m) (Proposed model)
Soil type 1 $k = 1.97 \times 10^{-4}$ m/s	1	3.5	6.5	$3.0 \times 10^{-3}$	0.0875	0.1070
	2	4.5	3.5	$6.0 \times 10^{-3}$	0.0585	0.0704
	3	4.2	0.5	$8.0 \times 10^{-3}$	0.126	0.0821
	4	3.2	3.0	$1.7 \times 10^{-3}$	0.192	0.1322
Soil type 2 $k = 2.23 \times 10^{-3}$ m/s	1	3.1	2.1	$3.0 \times 10^{-3}$	0.5857	0.4648
	2	2.2	5.5	$6.0 \times 10^{-3}$	0.1751	0.1691
	3	3.8	7.7	$8.0 \times 10^{-3}$	0.1311	0.1692
	4	4.3	5.0	$2.7 \times 10^{-2}$	0.1514	0.1150
Soil type 3 $k = 3.0 \times 10^{-6}$ m/s	1	4.7	2.6	$3.0 \times 10^{-3}$	0.0141	0.0097
	2	4.4	4.5	$6.0 \times 10^{-3}$	0.0044	0.0047
	3	3.1	2.8	$8.0 \times 10^{-3}$	0.0031	0.0043
	4	2.6	4.2	$1.2 \times 10^{-3}$	0.0104	0.0076



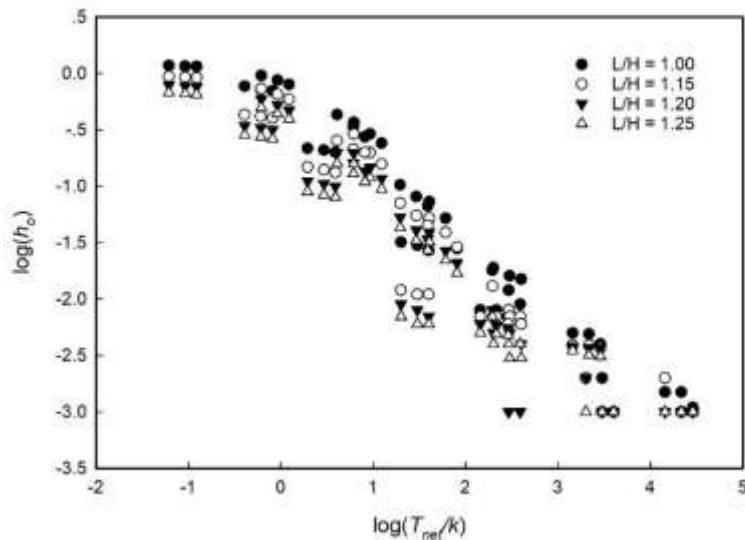
**Fig 1.** Plaxis model of mesh discretization with  $h_o$  and the relevant shape parameters of MSE wall with back drain using geocomposite (adopted from Chinkulkijniwat et al. 2016).



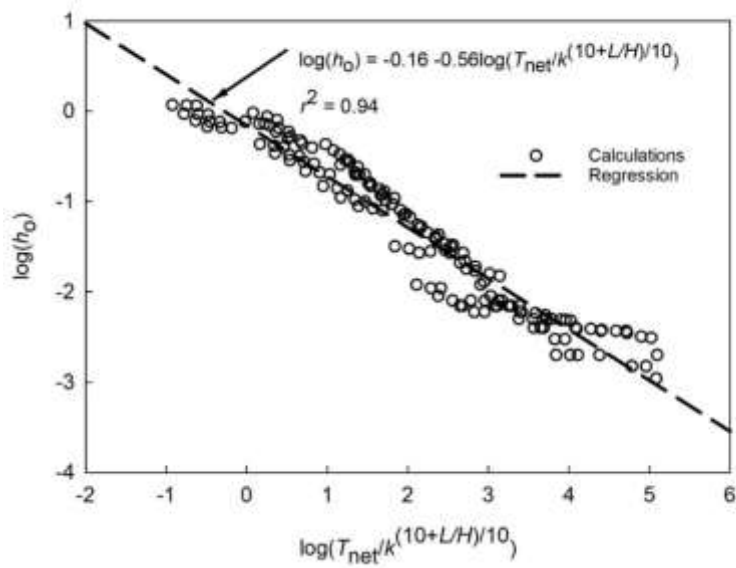
**Fig. 2.** Linear relationship of  $h_o$  subject to  $\log T_{net}$  and various shape parameter  $L$  values for (a) coarse sand, (b) sandy soil and (c) clayey sand (e) lateritic soil, and (f) clay.



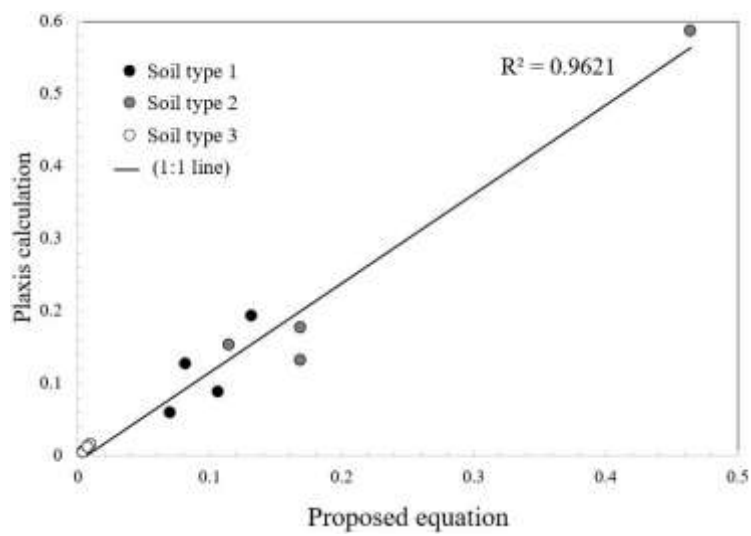
**Fig. 2 (cont.).** Linear relationship of  $h_o$  subject to  $\log T_{net}$  and various shape parameter  $L$  values for (a) coarse sand, (b) sandy soil and (c) clayey sand (e) lateritic soil, and (f) clay.



**Fig 3.** Variation of  $\log h_o$  and  $\log (T_{net}/k)$  for various  $L/H$  ratios



**Fig 4.** Relationship between  $\log h_o$  and  $\log (T_{net}/k^{(10+L/H)/10})$  and regression result



**Figure 5.** Comparison between  $h_o$  calculated from Plaxis and that from proposed equation.